ECON 257 EXERCISES 7

Classical linear model: Analysis of residuals Review questions

In the context of the classical linear regression model,

$$y = X\beta + \varepsilon$$
 , $\varepsilon \sim N[0, \sigma^2 I_T]$ (1)

$$y : T \times 1, \quad X : T \times k, \quad \varepsilon : T \times 1$$
 (2)

we wish to analyze whether the least squares residuals

$$\hat{\varepsilon} = y - X\hat{\beta} \tag{3}$$

behave as expected under the assumption that the model is correctly specified.

- 1. Establish the mean and covariance matrix of $\hat{\epsilon}$.
- 2. What is the distribution of $\hat{\epsilon}$?
- 3. Do the elements of $\hat{\varepsilon}$ have the same variance ? If not, propose a method for making all these variances equal.
- 4. Are the elements of $\hat{\varepsilon}$ uncorrelated ?
- 5. Propose a method for deciding whether a given residual is surprisingly "large".
- 6. Propose a method for deciding whether the residuals of the model contain an "outlier"?
- 7. Propose a method for testing the errors are "homoskedastic" against an alternative where the variance is increasing with the observation index (t = 1, ..., T).